

# Modeling of the Effect of MgO and ZrO<sub>2</sub> on Sintering of Alumina

H. K.H.Al.Mayaly

Department of physics, College of Education IbnAl-Haitham, University of Baghdad

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## Abstract

This research studies the effect of MgO and ZrO<sub>2</sub> as additives in sintering Al<sub>2</sub>O<sub>3</sub> . The experimental results are modeled using ( L<sup>2</sup> \_ regression) technique , sintered density and grain size rate measurements were accounted by utilizing experimental results of undoped , MgO doped and ZrO<sub>2</sub> doped alumina impregnated with spherical large pores in final stage of sintering . The effect of each additive is inhibition of the grain growth and increasing the densification rate which enhances the kinetics of densification and the removal of large and small pores.

## Introduction

Alumina ceramic (Al<sub>2</sub>O<sub>3</sub>) is a hard refractory ceramic, which has been used in high temperature, structural and substrate applications because of its good strength and low thermal expansion coefficient . Nevertheless , like other mono lithic ceramics, Al<sub>2</sub>O<sub>3</sub> is aptto suffer from low ductility and low fracture toughnees[I].

Doped samples were studied fro the influence of varying the grain growth rate of the alumina , MgO is a strong solid-solution grain growth inhibitor in high purity alumina [2] , and ZrO<sub>2</sub> when added in high enough concentrations, is an even strong second-phase grain growth inhibitor [3] .

The intension of this study to was model mathematically the densification and grain size rate of doped Al<sub>2</sub>O<sub>3</sub> system using regression modeling technique utilizing MgO and ZrO<sub>2</sub> as additives seperately.

### Theoretical background

The pores are classified into two basic types, there are the so-called matrix or first-generation pore and the second type, large so-called second-generation pores which originate from particulate agglomeration and particulate packing irregularities within the powder compact [4]. The large pores are always more difficult to eliminate large voids for two basic reasons. First, simple kinetics dictates a longer time to fill a larger void by diffusion [5], second a large pore can be thermodynamically stable depending on the value of dihedral angle and pore size : grain size ratio (for a given dihedral angle and pore size, there is a critical grain size above which the pore is unstable and can sinter), while below where it is stable and can not sinter.

The models which are used in this study have simplifying assumptions in order to perform the calculations.

- 1) Pore shrinkage is controlled by lattice diffusion
- 2) The grain size is fixed at the critical grain size which was taken to be 0.68 times the pore size [6].
- 3) The pores are assumed to be spherical with no thermodynamic barrier for shrinkage [4,7].

The large-pore volume will start to decrease (once the critical grain size is reached), the matrix grain growth rate (dG/dt) can be given by [8]

$$\frac{dG}{dt} = \frac{13.4}{N} M_p G \gamma_b \epsilon \left(1 - \frac{G}{G_{max}}\right) \dots (1)$$

Where N is the number of pores surrounding each grain,  $M_p$  is the average pore mobility, G is the grain size,  $\gamma_b$  is the grain boundary energy,  $\epsilon$  is the grain growth rate factor and (G/G<sub>max</sub>) is the ratio of average grain size over maximum grain size.

The densification rate (dp/dt) depends on the diffusion coefficient responsible for densification (D<sub>lattice</sub> or D<sub>boundary</sub>) and the grain size [9].

$$\frac{d\rho}{dt} = C D / G^n \dots (2)$$

where C is a constant and D is the diffusion coefficient.

The grain size exponent, n, is 3 for lattice- diffusion controlled densification which is used in this study [5].

In this study (reported in Ref [5]). Ultra-high-purity  $\alpha$ -alumina powder for which the manufacturer claimed a (99.995%) purity size of powder was 0.45  $\mu_m$  and 97% of the particles were less than 1  $\mu_m$ .

The following three compositions were chosen for this study (i) pure alumina ; (ii) 250-ppm-MgO-doped alumina , and (iii) Al<sub>2</sub>O<sub>3</sub> +10 Vol % ZrO<sub>2</sub> . Large mono size pores were introduced in to each composition by incorporating latex spheres (5.6 μ<sub>m</sub>) into the powder mix before sintering .The ratio of the sphere volume / the sum of the sphere volume and the solid volume in each composition was (5%) .The powder was cold-pressed into pellets of approximately the same green density (47.5%) using a high-purity alumina punch and die set . The pellets calcined at 1000<sup>o</sup>c in air for 48 h , large pores were produced after calcination as a result of burning out of the latex spheres.

The processing procedure for all composition was kept as consistent as possible to ensure similar initial microstructures . Sintering was conducted under flowing nitrogen gas in a furnace heated with graphite elements, the specimens were heated at a constant rate of (60<sup>o</sup>c/min) up to the sintering temperature of 1620<sup>o</sup>c (oxygen partial pressure < 10<sup>-11</sup> atm <10<sup>-6</sup> pa ).

**Regression modeling technique**

The equation of L<sup>2</sup>\_ regression which is used in this study can be express as follows [10]

$$X = (A^T A)^{-1} A^T b \dots\dots\dots(3)$$

where A is the matrix , A<sup>T</sup> is the transpose of matrix A , b is random observation and X is the fixed part of equation but unknown.

The integral form of the grain growth rate equation (1) [4].

$$\ln G_{t+\Delta t} - \ln G_t = \frac{13.4}{N} M_p Y_b \varepsilon (1 - \frac{G}{G_{max}}) \Delta t \dots\dots\dots(4)$$

and the integral form of densification rate equation (2)

$$\rho_{t+\Delta t} - \rho_t = \frac{CD}{(1 - n)} G^{(1-n)} \Delta t \dots\dots\dots(5)$$

After simplifying the integral expression for equation (4) and (5) we get a suitable form of equation (3) that can be adopted to L<sup>2</sup>\_ regression .

$$\ln G_{t+\Delta t} = z_1 (1 - \frac{G}{G_{max}})t + Y_1 \dots\dots\dots(6)$$

$$\rho_{t+\Delta t} = Z_2 G^{(1-n)} t + Y_2 \dots \dots \dots (7)$$

Where  $Z_1$  is the grain size rate parameter and equals to  $[\frac{13.4}{N} M_p Y_b \varepsilon]$ ,  $Z_2$  is the densification rate parameter and equals to  $[CD / (1-n)]$ ,  $Y_1$  is the grain size rate coefficient and equals to  $[\ln G_t - z_1 (1 - \frac{G}{G_{max}}) t_o]$  and  $Y_2$  is densification rate coefficient and equals to  $[P_t - Z_2 G^{1-n} t_o]$

The grain size and density value were measured using model of L<sup>2</sup> Regression (see-Ref II)

## Results and Disussion

Figs . (1) and (2) showed the effect of MgO and ZrO<sub>2</sub> doped alumina which have a large (□ 5 μ<sub>m</sub>) model spherical pores on the density date as a function of time at 1629°c . As can be seen that both MgO and ZrO<sub>2</sub> increased the desification rate of Al<sub>2</sub>O<sub>3</sub> . ZrO<sub>2</sub> had more effective in enhanced densification rate than MgO . The calculatedion by model sintered densites of sample with ZrO<sub>2</sub> addition was ranged between [ 92 and 97.9% ] and for samples with MgO addition was ranged between [ 91 and 97.2 % ] .

The ZrO<sub>2</sub>-doped samples did reach a slightly higher density than the MgO-doped samples , however , this does imply that a fraction of the pores were indeed thermodynamically unstable and cabable to shrink . Such pores would be able to shrink at a faster rate than those in the MgO – doped samples due to smaller grain size and associated faster kinetics.

Fig (3) and Fig (4) are showed the grain size versus time date for MgO-doped , and ZrO<sub>2</sub>-doped aluminas which imregnated with large (□ 5 μ<sub>m</sub>) model spherical pores at 1620 °c . MgO and ZrO<sub>2</sub> were very effective in inhibiting grain growth in the system (ZrO<sub>2</sub> more so than MgO), the grain sizes for undoped and MgO-doped samples well beyond the critical grain size and the large pores do not readily disapper even when thermodynamics is permitting .

The degree of grain growth inhibition was faster with the ZrO<sub>2</sub>-doped samples , where the small grain size of these samples showed that not all the pores were necessarily thermodynamically unstable for any reasonable lenght of sintering time.

In Table (1) we can see the grain size rate parameter of doping samples increases , this can be explained in terms of the number of pores which increase with doping and this may naturally decreases densification rate parameters .

Table (2) lists the grain size rate coefficient and densification rate coefficient, the doping lowers both the densification and grain size rate coefficient respectively where the dopant particles may form barriers along the diffusion path and reduce the densification

## Conclusion

The modeling technique shows that the calculated results using  $L^2$  Regression technique agrees with experimental results, and MgO-doped alumina impregnated with large pores have effective in inhibiting grain growth rate and increases the densification rate, while the effect of ZrO<sub>2</sub> doped alumina was faster than MgO, ZrO<sub>2</sub> doped samples have more effective in enhanced densification and inhibition the grain growth rate.

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**Table (1): Grain size and densification rate parameters in three case , undoped, MgO-doped and ZrO<sub>2</sub>-doped alumina impregted with large model pores**

	Undoped	MgO-doped	ZrO <sub>2</sub> -doped
Grain size rate parameter (Z <sub>1</sub> )	90.583	93.964	94.651
Densification rate parameter (Z <sub>2</sub> )	1.574	1.102	0.578

**Table (2): Grain size and densification rate coefficent in three case , undoped , MgO-doped and ZrO<sub>2</sub> –doped alumina impregnated with large model pores**

	Undoped	MgO-doped	ZrO <sub>2</sub> -doped
Grain size rate coefficient (Y <sub>1</sub> )	0.00559	0.00511	0.00238
Densification rate coefficient (Y <sub>2</sub> )	4.397	0.6562	0.0604

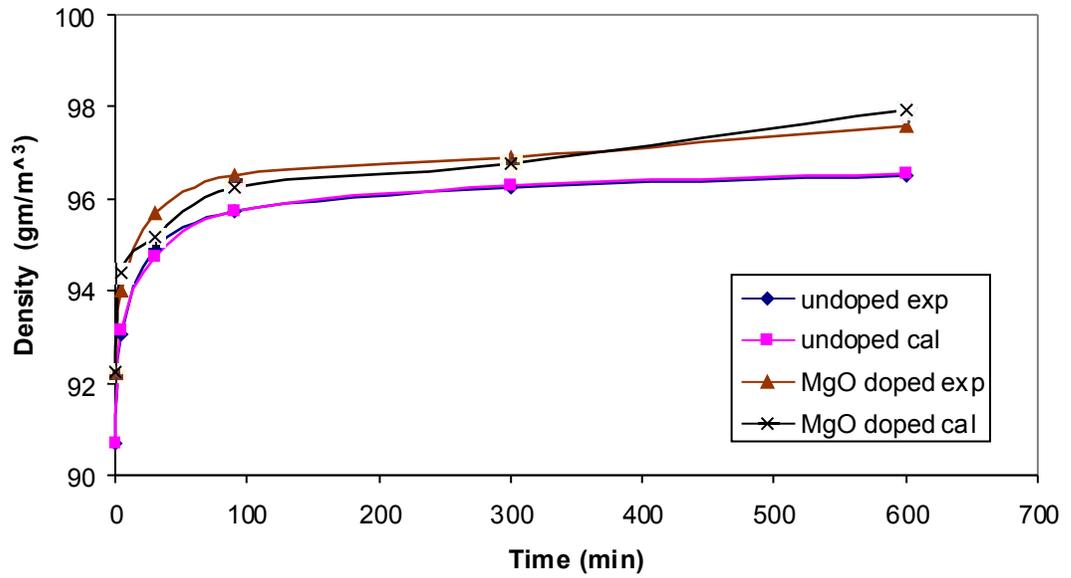
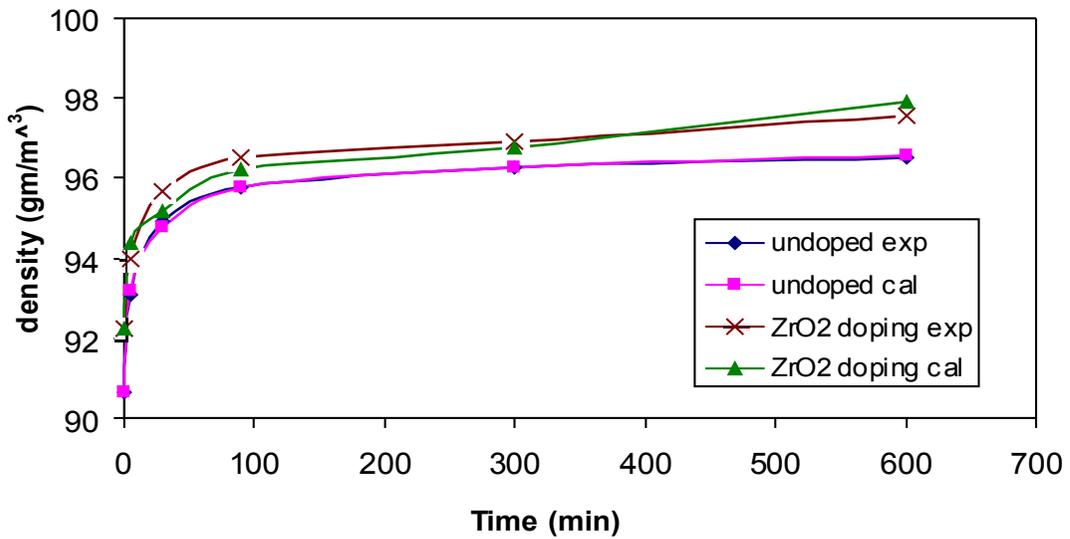


Fig (1) Density data of undoped and MgO doped aluminas impregnated with large pores as a function of time



Fig(2) Density data of undoped and ZrO<sub>2</sub> doped aluminas impregnated with large pores as a function of time

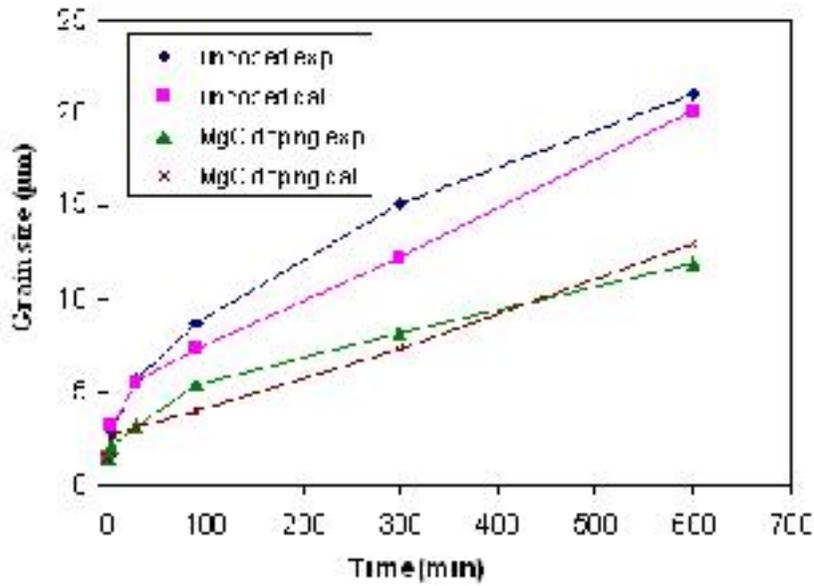


Fig. (3) Grain size of undoped and MgO-doped aluminas impregnated with large spherical pores as a function of time

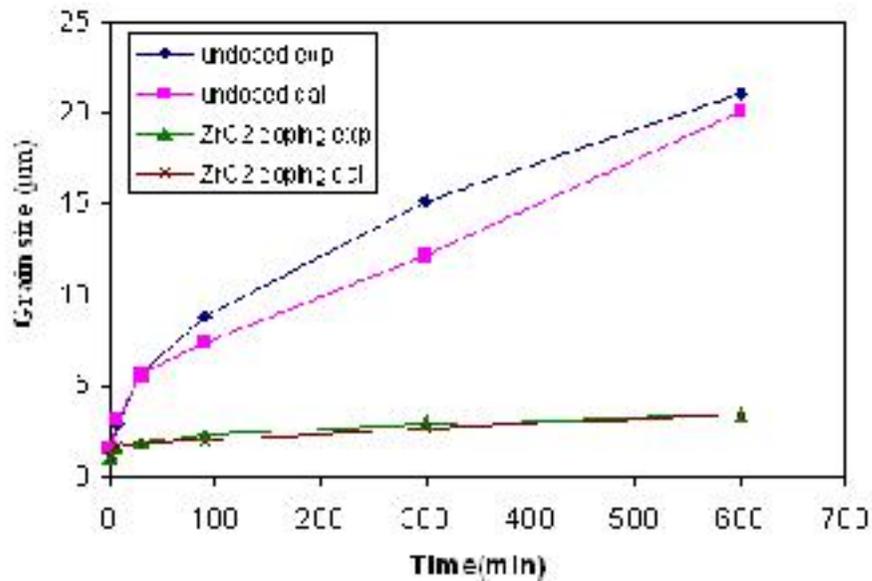


Fig. (4) Grain size of undoped and ZrO<sub>2</sub>-doped aluminas impregnated with large spherical pores as a function of time

## أنموذج تأثير MgO و ZrO<sub>2</sub> في تليبيد الالومينا

حنان كاظم حسون

قسم الفيزياء ، كلية التربية - ابن الهيثم ، جامعة بغداد

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قبل البحث في 17 حزيران 2010

### الخلاصة :-

درس تأثير اضافة MgO, ZrO<sub>2</sub> في تليبيد الالومينا. تم نمذجت النتائج التجريبية بأستخدام تقنية L2-Regression، وحسب معدل كثافة التليبيد والحجم الحبيبي بأستخدام نتائج تجريبية للأومينا غير مطعمة، المطعمة ب MgO والمطعمة ب ZrO<sub>2</sub> والمشبعة بالفجوات الكبيرة في المرحلة النهائية من عملية التليبيد. ان تأثير نوعي التطعيم هو منع النمو الحبيبي وزيادة معدل التكاثر حيث زيادة حركيات التكاثر وحركة الفجوات الكبيرة والصغيرة.

